

# BRIGHT CAREER SCIENCE ACADEMY

## DERIVATIVES FORMULAS & RULES

$\frac{d}{dx} x^n = nx^{n-1}$ Where $n \in R$	<b>Power Rule</b> $\frac{d}{dx} [f]^n = n[f]^{n-1} \cdot \frac{d}{dx} f$	<b>Product Rule</b> $\frac{d}{dx} [f \cdot g] = \left[ \frac{d}{dx} f \right] \cdot g + f \cdot \left[ \frac{d}{dx} g \right]$	$\frac{dx}{dx} = 1$ OR $\frac{d}{dx} (x) = 1$
<b>Quotient Rule</b> $\frac{d}{dx} \left[ \frac{f}{g} \right] = \frac{g \cdot \left[ \frac{d}{dx} f \right] - f \cdot \left[ \frac{d}{dx} g \right]}{[g]^2}$	$\frac{d}{dx} \sqrt{f} = \frac{1}{2\sqrt{f}} \cdot \left[ \frac{d}{dx} f \right]$	$\frac{dc}{dx} = 0$ OR $\frac{d}{dx} (c) = 0$ Where "c" is constant	$\frac{d}{dx} c \cdot f(x) = c \frac{d}{dx} f(x)$ Where "c" is constant
$\frac{d}{dx} \sin u = \cos u \cdot \frac{du}{dx}$	$\frac{d}{dx} \sinh u = \cosh u \cdot \frac{du}{dx}$	$\frac{d}{dx} \sin^{-1} u = \frac{1}{\sqrt{1-u^2}} \cdot \frac{du}{dx}$	$\frac{d}{dx} \sinh^{-1} u = \frac{1}{\sqrt{1+u^2}} \cdot \frac{du}{dx}$
$\frac{d}{dx} \cos u = -\sin u \cdot \frac{du}{dx}$	$\frac{d}{dx} \cosh u = \sinh u \cdot \frac{du}{dx}$	$\frac{d}{dx} \cos^{-1} u = \frac{-1}{\sqrt{1-u^2}} \cdot \frac{du}{dx}$	$\frac{d}{dx} \cosh^{-1} u = \frac{1}{\sqrt{u^2-1}} \cdot \frac{du}{dx}$
$\frac{d}{dx} \tan u = \sec^2 u \cdot \frac{du}{dx}$	$\frac{d}{dx} \tanh u = \text{sech}^2 u \cdot \frac{du}{dx}$	$\frac{d}{dx} \tan^{-1} u = \frac{1}{1+u^2} \cdot \frac{du}{dx}$	$\frac{d}{dx} \tanh^{-1} u = \frac{1}{1-u^2} \cdot \frac{du}{dx}$
$\frac{d}{dx} \text{cosec} u = -\text{cosec} u \cdot \cot u \cdot \frac{du}{dx}$	$\frac{d}{dx} \text{cosech} u = -\text{cosech} u \cdot \coth u \cdot \frac{du}{dx}$	$\frac{d}{dx} \text{cosec}^{-1} u = \frac{-1}{ u \sqrt{u^2-1}} \cdot \frac{du}{dx}$	$\frac{d}{dx} \text{cosech}^{-1} u = \frac{-1}{u\sqrt{1+u^2}} \cdot \frac{du}{dx}$
$\frac{d}{dx} \sec u = \sec u \cdot \tan u \cdot \frac{du}{dx}$	$\frac{d}{dx} \text{sech} u = -\text{sech} u \cdot \tanh u \cdot \frac{du}{dx}$	$\frac{d}{dx} \sec^{-1} u = \frac{1}{ u \sqrt{u^2-1}} \cdot \frac{du}{dx}$	$\frac{d}{dx} \text{sech}^{-1} u = \frac{-1}{u\sqrt{1-u^2}} \cdot \frac{du}{dx}$
$\frac{d}{dx} \cot u = -\text{cosec}^2 u \cdot \frac{du}{dx}$	$\frac{d}{dx} \coth u = -\text{cosech}^2 u \cdot \frac{du}{dx}$	$\frac{d}{dx} \cot^{-1} u = \frac{-1}{1+u^2} \cdot \frac{du}{dx}$	$\frac{d}{dx} \coth^{-1} u = \frac{1}{1-u^2} \cdot \frac{du}{dx}$
$\frac{d}{dx} e^u = e^u \cdot \frac{du}{dx}$	$\frac{d}{dx} a^u = a^u \cdot \ln a \cdot \frac{du}{dx}$	$\frac{d}{dx} \ln u = \frac{1}{u} \cdot \frac{du}{dx}$	$\frac{d}{dx} \log_a u = \frac{1}{u \ln a} \cdot \frac{du}{dx}$

## INTEGRATION FORMULAS & RULES

$\int x^n dx = \frac{x^{n+1}}{n+1}$ Where $n \neq -1$	$\int \frac{f'}{f} dx = \ln  f $	$\int f^n \cdot f' dx = \frac{f^{n+1}}{n+1}$ Where $n \neq -1$	$\int 1 dx = x$
$\int \sin ax dx = \frac{-\cos ax}{\frac{d}{dx} (ax)}$	$\int e^{ax} dx = \frac{e^{ax}}{\frac{d}{dx} (ax)}$	<b>Integration By Parts Rule</b> $\int f \cdot g dx = f \cdot \int g dx - \int \left( \frac{d}{dx} f \cdot \int g dx \right) dx$	$\int c f(x) dx = c \int f(x) dx$
$\int \cos ax dx = \frac{\sin ax}{\frac{d}{dx} (ax)}$	$\int a^{f(x)} dx = \frac{a^{f(x)}}{\ln a \cdot \frac{d}{dx} f(x)}$	$\int \text{cosec} ax \cdot \cot ax dx = \frac{-\text{cosec} ax}{\frac{d}{dx} (ax)}$	$\int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a}$
$\int \tan ax dx = \frac{\ln  \sec ax }{\frac{d}{dx} (ax)}$ OR $\frac{-\ln  \cos ax }{\frac{d}{dx} (ax)}$	$\int \text{cosec}^2 ax dx = \frac{-\cot ax}{\frac{d}{dx} (ax)}$	$\int \sec ax \cdot \tan ax dx = \frac{\sec ax}{\frac{d}{dx} (ax)}$	$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a}$
$\int \text{cosec} ax dx = \frac{\ln  \text{cosec} ax - \cot ax }{\frac{d}{dx} (ax)}$	$\int \sec^2 ax dx = \frac{\tan ax}{\frac{d}{dx} (ax)}$	<b>Fundamental theorem of calculus</b> $\int_a^b f(x) dx = F(b) - F(a)$	$\int \frac{dx}{\sqrt{x^2 - a^2}} = \ln \left( x + \sqrt{x^2 - a^2} \right)$
$\int \sec ax dx = \frac{\ln  \sec ax + \tan ax }{\frac{d}{dx} (ax)}$	$\int \sqrt{a^2 - x^2} = \frac{a^2}{2} \sin^{-1} \frac{x}{a} + \frac{x}{2} \sqrt{a^2 - x^2}$	<b>Property of Definite Integral</b> $\int_a^b f(x) dx = - \int_b^a f(x) dx$	$\int \frac{dx}{a^2 - x^2} = \frac{1}{2a} \ln \left  \frac{a+x}{a-x} \right $
$\int \cot ax dx = \frac{\ln  \sin ax }{\frac{d}{dx} (ax)}$	$\int e^{ax} [a \cdot f(x) + f'(x)] dx = e^{ax} \cdot f(x)$	<b>Property of Definite Integral</b> $\int_a^b f(x) dx = \int_a^c f(x) dx + \int_c^b f(x) dx$ Where $a < c < b$	$\int \frac{dx}{x^2 - a^2} = \frac{1}{2a} \ln \left  \frac{x-a}{x+a} \right $

Note: Add Integration Constant "c" with Every Indefinite Integration Formula

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